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## Directional limits on persistent gravitational waves using LIGO S5 science data

LIGO Scientific Collaboration ; Virgo Collaboration ; Abadie, J ; Bondarescu, R

**Abstract:** The gravitational-wave (GW) sky may include nearby pointlike sources as well as astrophysical and cosmological stochastic backgrounds. Since the relative strength and angular distribution of the many possible sources of GWs are not well constrained, searches for GW signals must be performed in a model-independent way. To that end we perform two directional searches for persistent GWs using data from the LIGO S5 science run: one optimized for pointlike sources and one for arbitrary extended sources. The latter result is the first of its kind. Finding no evidence to support the detection of GWs, we present 90% confidence level (CL) upper-limit maps of GW strain power with typical values between  $2\text{--}20 \times 10^{-50} \text{ strain}^2 \text{ Hz}^{-1}$  and  $5\text{--}35 \times 10^{-49} \text{ strain}^2 \text{ Hz}^{-1} \text{ sr}^{-1}$  for pointlike and extended sources respectively. The limits on pointlike sources are shown for  $\text{bandroot} - \text{mean} - \text{square}$  GW strain from interesting targets including  $\text{ScoX-1}$ ,  $\text{SN1987A}$  and the Galactic Center as well as for extended sources.

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# Directional limits on persistent gravitational waves using LIGO S5 science data

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The gravitational-wave (GW) sky may include nearby pointlike sources as well as astrophysical and cosmological stochastic backgrounds. Since the relative strength and angular distribution of the many possible sources of GWs are not well constrained, searches for GW signals must be performed in a model-independent way. To that end we perform two directional searches for persistent GWs using data from the LIGO S5 science run: one optimized for pointlike sources and one for arbitrary extended sources. The latter result is the first of its kind. Finding no evidence to support the detection of GWs, we present 90% confidence level (CL) upper-limit maps of GW strain power with typical values between  $2 - 20 \times 10^{-50} \text{ strain}^2 \text{ Hz}^{-1}$  and  $5 - 35 \times 10^{-49} \text{ strain}^2 \text{ Hz}^{-1} \text{ sr}^{-1}$  for pointlike and extended sources respectively. The limits on pointlike sources constitute a factor of 30 improvement over the previous best limits. We also set 90% CL limits on the narrow-band root-mean-square GW strain from interesting targets including Sco X-1, SN1987A and the Galactic Center as low as  $\approx 7 \times 10^{-25}$  in the most sensitive frequency range near 160 Hz. These limits are the most constraining to date and constitute a factor of 5 improvement over the previous best limits.

## I. INTRODUCTION

One of the most ambitious goals of gravitational-wave (GW) astronomy is to measure the stochastic cosmological gravitational-wave background (CGB), which can arise through a variety of mechanisms including amplification of vacuum fluctuations following inflation [1], phase transitions in the early universe [2, 3], cosmic strings [4, 5] and pre-Big Bang models [6, 7]. The CGB may be masked by an astrophysical gravitational-wave background (AGB), interesting in its own right, which can arise from the superposition of unresolved sources such as core-collapse supernovae [8, 9], neutron-star excitations [10, 11], binary mergers [12, 13], persistent emission from neutron stars [14, 15] and compact objects around supermassive black holes [16, 17].

We present the results of two analyses using data from the LIGO S5 science run: a radiometer analysis optimized for pointlike sources and a spherical-harmonic decomposition analysis, which allows for arbitrary angular distributions. This work presents the first measurement of the GW sky in a framework consistent with an arbitrary extended source.

## II. LIGO DETECTORS AND THE S5 SCIENCE RUN

We analyze data from LIGO's 4 km and 2 km detectors (H1 and H2) in Hanford, WA and the 4 km detector (L1) in Livingston Parish, LA during the S5 science run, which took place between Nov. 5, 2005 and Sep. 30, 2007. During S5, both H1 and L1 reached a strain sensitivity of  $3 \times 10^{-23} \text{ strain Hz}^{-1/2}$  in the most sensitive region between 100 – 200 Hz [18] and collected 331 days of coincident H1L1 and H2L1 data. S5 saw milestones in GW astronomy including limits on the emission of GWs from the Crab pulsar that surpass those inferred from the Crab's spindown [19], as well as limits on the isotropic CGB that surpass indirect limits from Big Bang nucleosynthesis and the cosmic microwave background [20]. This work builds on [20, 21].

## III. METHODOLOGY

Following [21, 22] we present a framework for analyzing the angular distribution of GWs. We assume that the GW signal is stationary and unpolarized, but not necessarily isotropic. It follows that the GW energy density  $\Omega_{\text{GW}}(f)$ , can be expressed in terms of the GW power

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spectrum,  $\mathcal{P}(f, \hat{\Omega})$ :

$$\Omega_{\text{GW}}(f) \equiv \frac{f}{\rho_c} \frac{d\rho_{\text{GW}}}{df} = \frac{2\pi^2}{3H_0^2} f^3 \int_{S^2} d\hat{\Omega} \mathcal{P}(f, \hat{\Omega}). \quad (1)$$

Here  $f$  is frequency,  $\hat{\Omega}$  is sky location,  $\rho_c$  is the critical density of the universe and  $H_0$  is Hubble's constant. We further assume that  $\mathcal{P}(f, \hat{\Omega})$  can be factored (in our analysis band) into an angular power spectrum,  $\mathcal{P}(\hat{\Omega})$ , and a spectral shape,  $\bar{H}(f) \equiv (f/f_0)^\beta$ , parameterized by the spectral index  $\beta$  and reference frequency  $f_0$ . We set  $f_0 = 100$  Hz to be in the sensitive range of the LIGO interferometers.

Our goal is to measure  $\mathcal{P}(\hat{\Omega})$  for two power-law signal models. In the cosmological model,  $\beta = -3$  ( $\Omega_{\text{GW}}(f) = \text{const}$ ), which is predicted, e.g., for the amplification of vacuum fluctuations following inflation (see [23] and references therein). In the astrophysical model,  $\beta = 0$  ( $\bar{H}(f) = \text{const}$ ), which emphasizes the strain sensitivity of the LIGO detectors.

We estimate  $\mathcal{P}(\hat{\Omega})$  two ways. The *radiometer algorithm* [21, 24, 25] assumes the signal is a point source characterized by a single direction  $\hat{\Omega}_0$  and amplitude,  $\eta(\hat{\Omega}_0)$ :

$$\mathcal{P}(\hat{\Omega}) \equiv \eta(\hat{\Omega}_0) \delta^2(\hat{\Omega}, \hat{\Omega}_0). \quad (2)$$

It is applicable to a GW sky dominated by a limited number of widely separated point sources. As the number of point sources is increased, however, the interferometer beam pattern will cause the signals to interfere and partly cancel. Thus, radiometer maps do not apply to extended sources. Since pointlike signals are expected to arise from astrophysical sources, we use  $\beta = 0$  for the radiometer analysis.

The *spherical-harmonic decomposition (SHD) algorithm* is used for both  $\beta = -3$  (cosmological) and  $\beta = 0$  (astrophysical) sources. It allows for the possibility of an extended source with an arbitrary angular distribution, characterized by spherical-harmonic coefficients  $\mathcal{P}_{lm}$  such that

$$\mathcal{P}(\hat{\Omega}) \equiv \sum_{lm} \mathcal{P}_{lm} Y_{lm}(\hat{\Omega}). \quad (3)$$

The series is cut off at  $l_{\text{max}}$ , allowing for angular scale  $\sim 2\pi/l_{\text{max}}$ . The flexibility of the spherical-harmonic algorithm comes at the price of somewhat diminished sensitivity to point sources, and thus the two algorithms are complementary.

We choose  $l_{\text{max}}$  so as to minimize the sky average of the product of  $\sigma(\hat{\Omega})$  and  $\bar{A}$ , where  $\sigma(\hat{\Omega})$  is the uncertainty associated with  $\mathcal{P}(\hat{\Omega})$  and  $\bar{A}$  is the typical angular area of a resolved patch of sky [37]. Since  $\bar{A} = 4\pi/N_{\text{indep}} \propto 1/(l_{\text{max}} + 1)^2$  (where  $N_{\text{indep}}$  is the number of independent parameters), this procedure amounts to choosing  $l_{\text{max}}$  to maximize the sensitivity obtained by integrating over the typical search aperture (angular resolution). We obtain  $l_{\text{max}} = 7$  and 12 for  $\beta = -3$  and  $\beta = 0$ , respectively.

Since the search aperture becomes smaller at the higher frequencies emphasized by  $\beta = 0$ ,  $l_{\text{max}}$  is larger for  $\beta = 0$  than for  $\beta = -3$ .

Both algorithms can be framed in terms of a “dirty map”,  $X_\nu$ , which represents the signal convolved the Fisher matrix,  $\Gamma_{\mu\nu}$ :

$$X_\nu = \sum_{ft} \gamma_\nu^*(f, t) \frac{\bar{H}(f)}{P_1(f, t) P_2(f, t)} C(f, t) \quad (4)$$

$$\Gamma_{\mu\nu} = \sum_{ft} \gamma_\mu^*(f, t) \frac{\bar{H}^2(f)}{P_1(f, t) P_2(f, t)} \gamma_\nu(f, t). \quad (5)$$

Here both the Greek indices  $\mu$  and  $\nu$  take on values of  $lm$  for the SHD algorithm and  $\hat{\Omega}$  for the radiometer algorithm, for which we use the pixel basis. The two bases are related using spherical-harmonic basis functions:

$$X_{\hat{\Omega}} = \sum_{lm} X_{lm} Y_{lm}(\hat{\Omega}). \quad (6)$$

$C(f, t)$ , meanwhile, is the cross spectral density generated from the H1L1 or H2L1 pairs.  $P_1(f, t)$  and  $P_2(f, t)$  are the individual power spectral densities, and  $\gamma_\mu(f, t)$  is the angular decomposition of the overlap reduction function  $\gamma(\hat{\Omega}, f, t)$ , which characterizes the orientations and frequency response of the detectors [22]:

$$\gamma_\mu(f, t) \equiv \int_{S^2} d\hat{\Omega} \gamma(\hat{\Omega}, f, t) \mathbf{e}_\mu(\hat{\Omega}) \quad (7)$$

$$\gamma(\hat{\Omega}, f, t) = \frac{1}{2} F_1^A(\hat{\Omega}, t) F_2^A(\hat{\Omega}, t) e^{i2\pi f \hat{\Omega} \cdot (\Delta \vec{x}_{12}(t))/c}. \quad (8)$$

Here  $F_I^A(\hat{\Omega}, t)$  characterizes the detector response of detector  $I$  to a GW with polarization  $A$ ,  $\mathbf{e}_\mu(\hat{\Omega})$  is a basis function,  $c$  is the speed of light and  $\Delta \vec{x}_{12} \equiv \vec{x}_1 - \vec{x}_2$  is the difference between the interferometer locations. A detailed discussion of these quantities can be found in [22].

In [22] it was shown that the maximum-likelihood estimators of GW power are given by  $\hat{\mathcal{P}} = \Gamma^{-1} X$ . The inversion of  $\Gamma$  is complicated by singular eigenvalues associated with modes to which the Hanford-Livingston (HL) detector network is insensitive. This singularity can be handled two ways. The radiometer algorithm assumes the signal is pointlike, implying that correlations between neighboring pixels can be ignored. Consequently, we can replace  $\Gamma^{-1}$  with  $(\Gamma_{\hat{\Omega}\hat{\Omega}})^{-1}$  to estimate the point source amplitude  $\eta(\hat{\Omega})$  (see Eq. 2). (We note that pointlike sources create signatures in our sky maps that typically span several degrees or more; see [21].)

The SHD algorithm, on the other hand, targets extended sources, so the full Fisher matrix must be taken into account. We regularize  $\Gamma$  by removing a fraction,  $\mathcal{F}$ , of the modes associated with the smallest eigenvalues, to which the HL network is relatively insensitive.  $\mathcal{F}$  is known as the regularization cutoff. By removing some modes from the Fisher matrix, we obtain a regularized inverse Fisher matrix,  $\Gamma_R^{-1}$ , thereby introducing a bias,

the implications of which are discussed below. For now, we note that the bias depends on the angular distribution of the signal.

We thereby obtain the estimators

$$\hat{\eta}_{\hat{\Omega}} = (\Gamma_{\hat{\Omega}\hat{\Omega}})^{-1} X_{\hat{\Omega}} \quad (9)$$

$$\hat{\mathcal{P}}_{lm} = \sum_{l'm'} (\Gamma_R^{-1})_{lm,l'm'} X_{l'm'}, \quad (10)$$

with uncertainties

$$\sigma_{\hat{\Omega}}^{\text{rad}} = (\Gamma_{\hat{\Omega}\hat{\Omega}})^{-1/2} \quad (11)$$

$$\sigma_{lm}^{\text{sph}} = [(\Gamma_R^{-1})_{lm,lm}]^{1/2}. \quad (12)$$

We refer to  $\hat{\mathcal{P}}_{\hat{\Omega}} \equiv \sum_{lm} \hat{\mathcal{P}}_{lm} Y_{lm}(\hat{\Omega})$  as the “clean map” and  $\hat{\eta}_{\hat{\Omega}}$  as the “radiometer map.” We note that  $\hat{\eta}_{\hat{\Omega}}$  has units of  $\text{strain}^2 \text{Hz}^{-1}$  whereas  $\hat{\mathcal{P}}_{\hat{\Omega}}$  has units of  $\text{strain}^2 \text{Hz}^{-1} \text{sr}^{-1}$ .

In choosing  $\mathcal{F}$  one must balance the competing demands of reconstruction accuracy (sensitivity to the modes that are kept) with the bias associated with the modes that are removed. In practice, we do not know the bias associated with  $\mathcal{F}$  since it depends on the unknown signal distribution  $\mathcal{P}(\hat{\Omega})$ . Therefore, we choose a value of  $\mathcal{F}$  that tends to produce reliably reconstructed maps with minimal bias for simulated signals. Following [22], we use  $\mathcal{F} = 1/3$ , which was shown to be a robust regularization cutoff for simulated signals including maps characterized by one or more point sources, dipoles, monopoles and an extended source clustered in the galactic plane (see [22]).

In the case of the SHD algorithm, we construct an additional statistic (see [22]),

$$\hat{C}_l \equiv \frac{1}{2l+1} \sum_m [|\hat{\mathcal{P}}_{lm}|^2 - (\Gamma_R^{-1})_{lm,lm}], \quad (13)$$

which describes the angular scale of the clean map. The subtracted second term makes the estimator unbiased so that  $\langle \hat{C}_l \rangle = 0$  when no signal is present. The expected noise distribution of  $\hat{C}_l$  is highly non-Gaussian for small values of  $l$ , and so the upper limits presented below are calculated numerically. The  $\hat{C}_l$  are analogous to similar quantities defined in the context of temperature fluctuations of the cosmic microwave background (see, e.g., [26]).

The analysis was performed using the S5 stochastic analysis pipeline. This pipeline has been tested with hardware and software injections, and the successful recovery of isotropic hardware injections is documented in [20]. The recovery of anisotropic software injections is demonstrated in [22]. We parse time series into 60s, Hann-windowed, 50%-overlapping segments, which are coarse-grained to achieve 0.25 Hz resolution. We apply a stationarity cut described in [21], which rejects  $\sim 3\%$  of the cross-correlated segments. We also mask frequency bins associated with instrumental lines (e.g., harmonics of the 60 Hz mains power, calibration lines and suspension-wire resonances) as well as injected, simulated pulsar signals. For  $\beta = -3, 0$  we include frequency

bins up to 200, 500 Hz, so that  $\sigma(\hat{\Omega})$  is within  $\lesssim 2\%$  of the minimum possible value. Thirty-three frequency bins are masked, corresponding to 2% of the frequency bins between 40 – 500 Hz used in the broadband analyses. For additional details about the S5 stochastic pipeline, see [20].

#### IV. SIGNIFICANCE AND UPPER LIMIT CALCULATIONS

In order to determine if there is a statistically significant GW signature, we are primarily interested in the significance of outliers—the highest signal-to-noise ratio (SNR) frequency bin or sky-map pixel. It is therefore necessary to calculate the expected noise probability distribution of the maximum SNR given many independent trials (when considering maximum SNR in a spectral band) and given many *dependent* trials (when considering maximum SNR for a sky map).

For  $N$  independent frequency bins, the probability density function,  $\pi(\rho_{\text{max}})$ , of maximum SNR,  $\rho_{\text{max}}$ , is given by

$$\pi(\rho_{\text{max}}) \propto \left[1 + \text{erf}\left(\rho_{\text{max}}/\sqrt{2}\right)\right]^{N-1} e^{-\rho_{\text{max}}^2/2}. \quad (14)$$

Here we have assumed that the stochastic point estimate is Gaussian distributed. The Gaussianity of  $\hat{\mathcal{P}}_{\hat{\Omega}}$  and  $\hat{\eta}_{\hat{\Omega}}$ , calculated by summing over many  $\mathcal{O}(500\text{K})$  independent segments, is expected to arise due to the central limit theorem [27]. Additionally, we find the Gaussian-noise hypothesis to be consistent with time-slide studies, wherein we perform the cross-correlation analysis with an unphysical time-shift in order to wash out astrophysical signals and thereby obtain different realizations of detector noise.

The distribution of maximum SNR for a sky map is more subtle due to the non-zero covariances that exist between different pixels (or patches) on the sky. For this case, we calculate  $\pi(\rho_{\text{max}})$  numerically, by simulating many realizations of dirty maps that have expected covariances described by the Fisher matrix  $\Gamma$ . Figure 1 shows the numerically determined  $\pi(\rho_{\text{max}})$  for the  $\beta = -3$  clean map generated with Gaussian noise.

The likelihood function for  $\mathcal{P}(\hat{\Omega})$  at each point in the sky can be described as a normal distribution with mean  $\hat{\mathcal{P}}_{\hat{\Omega}}$  and a variance  $(\sigma_{\hat{\Omega}}^{\text{sph}})^2$ . In the case of the SHD algorithm, regularization introduces a signal-dependent bias. Without knowing the true distribution of  $\mathcal{P}(\hat{\Omega})$ , it is impossible to know the bias exactly, but it is possible to set a conservative upper limit by assuming that on average the modes removed through regularization contain no more GW power than the modes that are kept.

To implement this assumption, we calculate  $\hat{\mathcal{P}}_{lm}$  with a regularization scheme that sets eigenvalues of removed modes to zero, whereas  $\sigma_{lm}^{\text{sph}}$  is conservatively calculated using a regularization scheme that sets eigenvalues of removed modes to the average eigenvalue of the kept

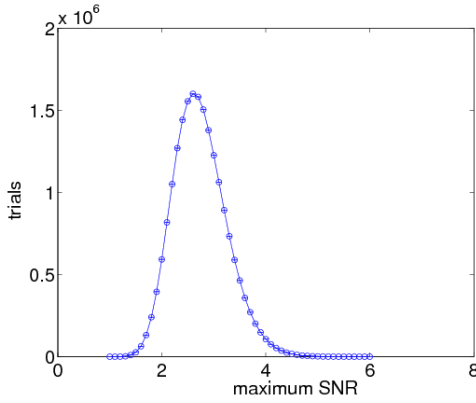


FIG. 1: Numerically calculated distribution of the maximum SNR for  $\beta = -3$  clean maps created from Gaussian noise.

modes. This has the effect of widening the likelihood function at each sky location. The upper limits become on average 25% larger than they would be if we had calculated  $\sigma_{lm}^{\text{sph}}$  using the same regularization scheme as  $\hat{\mathcal{P}}_{lm}$ .

Following the same procedure as in [20], we marginalize over the H1, H2, and L1 calibration uncertainties, which were measured to be 10%, 10%, and 13%, respectively [28] [38]. The posterior distribution is obtained by multiplying the marginalized likelihood function by a prior, which we take to be flat above  $\mathcal{P}(\hat{\Omega}) > 0$  [39]. The Bayesian upper limits are then determined by integrating the posterior out to the value of  $\mathcal{P}(\hat{\Omega})$  which includes 90% of the total area under the distribution. The calculation of upper limits on  $\eta_{\hat{\Omega}}$  is analogous except we need not take into account the effects of regularization.

## V. RESULTS

*Sky maps:* Figure 2 presents sky map results for the different analyses: SHD algorithm with  $\beta = -3$  (left), SHD with  $\beta = 0$  (center), and radiometer with  $\beta = 0$  (right). The top row contains SNR maps. The maximum SNR values are 3.1 (with significance  $p = 25\%$ ), 3.1 (with  $p = 56\%$ ), and 3.2 (with  $p = 53\%$ ) respectively. These  $p$ -values take into account the number of search directions and covariances between different sky patches (see IV). Observing no evidence of GWs, we set upper limits on GW power as a function of direction. The 90% confidence level (CL) upper limit maps are given in the bottom row. For the SHD method with  $\beta = -3$ , the limits are between  $5 - 31 \times 10^{-49} \text{ strain}^2 \text{ Hz}^{-1} \text{ sr}^{-1}$ ; for SHD with  $\beta = 0$ , the limits are between  $6 - 35 \times 10^{-49} \text{ strain}^2 \text{ Hz}^{-1} \text{ sr}^{-1}$ ; and for the radiometer with  $\beta = 0$ , the limits are between  $2 - 20 \times 10^{-50} \text{ strain}^2 \text{ Hz}^{-1}$ .

The strain power limits can also be expressed in terms

of the GW energy flux per unit frequency [21]:

$$\hat{F}(f, \hat{\Omega}) = \frac{c^3 \pi f_0^2}{4G} \left( \frac{f}{f_0} \right)^{\beta+2} \hat{\mathcal{P}}_{\hat{\Omega}} \quad (15)$$

$$= \left( 3.18 \times 10^{42} \frac{\text{erg}}{\text{cm}^2 \text{ s}} \right) \left( \frac{f}{100 \text{ Hz}} \right)^{\beta+2} \hat{\mathcal{P}}_{\hat{\Omega}}. \quad (16)$$

(Radiometer energy flux is obtained by replacing  $\hat{\mathcal{P}}_{\hat{\Omega}}$  with  $\hat{\eta}_{\hat{\Omega}}$ .) The corresponding values are  $2 - 10 \times 10^{-6} (f/100 \text{ Hz})^{-1} \text{ erg cm}^{-2} \text{ s}^{-1} \text{ Hz}^{-1} \text{ sr}^{-1}$  and  $2 - 11 \times 10^{-6} (f/100 \text{ Hz})^2 \text{ erg cm}^{-2} \text{ s}^{-1} \text{ Hz}^{-1} \text{ sr}^{-1}$  for the SHD method, and  $6 - 60 \times 10^{-8} (f/100 \text{ Hz})^2 \text{ erg cm}^{-2} \text{ s}^{-1} \text{ Hz}^{-1}$  for the radiometer. The radiometer map constitutes a factor of  $\sim 30$  improvement over the previous best strain power limits [21].

When comparing the SHD analysis with  $\beta = 0$  and the radiometer upper limits obtained using the same spectrum, it is important to note that these maps have different units. The radiometer map has units of  $\text{strain}^2 \text{ Hz}^{-1}$  because the radiometer analysis effectively integrates the power from a GW point source over solid angle. The SHD maps, on the other hand, have units of  $\text{strain}^2 \text{ Hz}^{-1} \text{ sr}^{-1}$ . If we scale the SHD limit maps by the typical diffraction limited resolution ( $\bar{A} \approx 0.1 \text{ sr}$ ), then the limits are more comparable. The radiometer algorithm limits are lower (by a factor of  $\lesssim 2$ ) because it requires a stronger assumption about the signal model (a single point source), whereas the SHD algorithm is model-independent.

Figure 3 show 90% CL upper limits on the  $C_l$ . Since the  $\mathcal{P}_{lm}$  have units of strain power ( $\text{strain}^2 \text{ Hz}^{-1} \text{ sr}^{-1}$ ), the  $C_l$  have the somewhat unusual units of  $\text{strain}^4 \text{ Hz}^{-2} \text{ sr}^{-2}$ .

*Targeted searches:* Sco X-1 is a nearby (2.8 kpc) low-mass X-ray binary likely to include a neutron star spun up through accretion. Its spin frequency is unknown. It has been suggested that this accretion torque is balanced by GW emission [29]. The Doppler line broadening due to the orbital motion is smaller than the chosen  $\delta f = 0.25 \text{ Hz}$  bin width for frequencies below  $\approx 930 \text{ Hz}$  [30]. At higher frequencies, the signal is certain to span two bins. We determine the maximum value of SNR in the direction of Sco X-1 to be 3.6 at  $f = 1770.50 \text{ Hz}$ , which has a significance of  $p = 73\%$  given the  $\mathcal{O}(7000)$  independent frequency bins. Thus in Fig. 4 (first panel) we present limits on root-mean-square (RMS) strain,  $h_{\text{RMS}}(f, \hat{\Omega})$ , as a function of frequency in the direction of Sco X-1 (RA, dec) = (16.3 hr, 15.6°). These limits improve on the previous best limits by a factor of  $\sim 5$  [21]. RMS strain is related to narrow-band GW power via

$$h_{\text{RMS}}(f, \hat{\Omega}) = \left[ \eta(f, \hat{\Omega}) \delta f \right]^{1/2}, \quad (17)$$

and is better suited for comparison with searches for periodic GWs, which typically constrain the peak strain amplitude,  $h_0$ , marginalized over neutron star parameters  $\iota$  and  $\psi$  (see, e.g., [31]). Our limits on  $h_{\text{RMS}}$  are for a circularly polarized signal from a pulsar whose spin axis is aligned with the line of sight. Marginalizing over



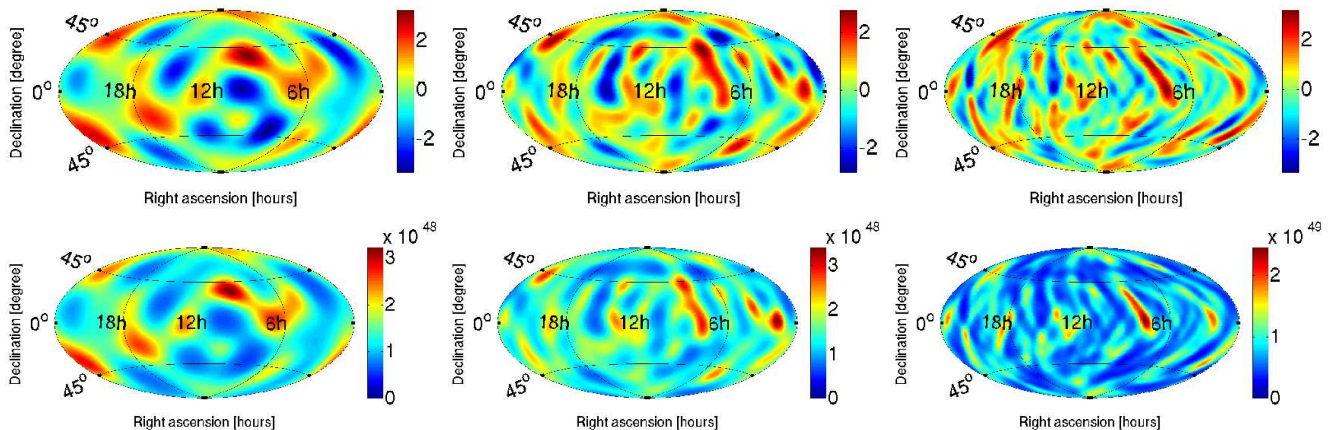


FIG. 2: Top row: Signal-to-noise ratio maps for the three different analyses described in this paper: SHD clean map for  $\beta = -3$  (left), SHD clean map for  $\beta = 0$  (center), and radiometer for  $\beta = 0$  (right). All three SNR maps are consistent with detector noise. The p-values associated with each map's maximum SNR are (from left to right)  $p = 25\%$ ,  $p = 56\%$ ,  $p = 53\%$ . Bottom row: The corresponding 90% CL upper limit maps on strain power in units of  $\text{strain}^2\text{Hz}^{-1}\text{sr}^{-1}$  for the SHD algorithm, and units of  $\text{strain}^2\text{Hz}^{-1}$  for the radiometer algorithm.

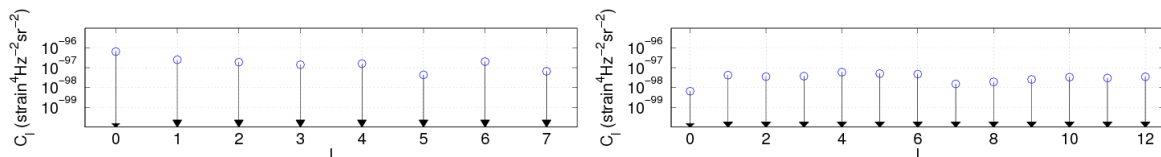


FIG. 3: Upper limits on  $C_l$  at 90% CL vs  $l$  for the SHD analyses for  $\beta = -3$  (left) and  $\beta = 0$  (right). The  $\hat{C}_l$  are consistent with detector noise.

$\iota$  and  $\psi$  and converting from RMS to peak amplitude causes the limits to change by a sky-dependent factor of  $\approx 2.3$  [32]. We note that these limits are on the RMS strain in each bin as opposed to the total RMS strain from Sco X-1, which might span as many as two bins. The frequency axis refers to the observed GW frequency as opposed to the intrinsic GW frequency.

We also look for statistically significant outliers associated with the Galactic Center (RA, dec) = (17.8 hr,  $-29^\circ$ ) and SN1987A (RA, dec) = (5.6 hr,  $-69^\circ$ ). The maximum SNR values are 3.5 at  $f = 203.25$  Hz with  $p = 85\%$  and 4.3 at 1367.25 Hz with  $p = 7\%$ , respectively. Limits on RMS strain are given in the right panel of Fig. 4.

## VI. CONCLUSIONS

We performed two directional analyses for persistent GWs: the radiometer analysis, which is optimized for point sources, and the complementary spherical-harmonic decomposition (SHD) algorithm, which allows for arbitrary extended sources. Neither analysis finds evidence of GWs. Thus we present upper-limit maps of GW power and also limits on the RMS strain from Sco X-1, the Galactic Center and SN1987A. The radiometer map limits improve on the previous best limits [21] by a fac-

tor of 30 in strain power, and limits on RMS strain from Sco X-1 constitute a factor of 5 improvement in strain over the previous best limits [21]. The SHD clean maps represent the first effort to look for anisotropic extended sources of GWs.

With the ongoing construction of second-generation GW interferometers, we are poised to enter a new era in GW astronomy. Advanced detectors [33–36] are expected to achieve strain sensitivities approximately 10 times lower than initial LIGO, and advances in seismic isolation are expected to extend the frequency band down from 40 Hz to 10 Hz [33]. By adding additional detectors to our network, we expect to reduce degeneracies in the Fisher matrix and improve angular resolution. These improvements will allow advanced detector networks to probe plausible models of astrophysical stochastic foregrounds and some cosmological models such as cosmic strings.

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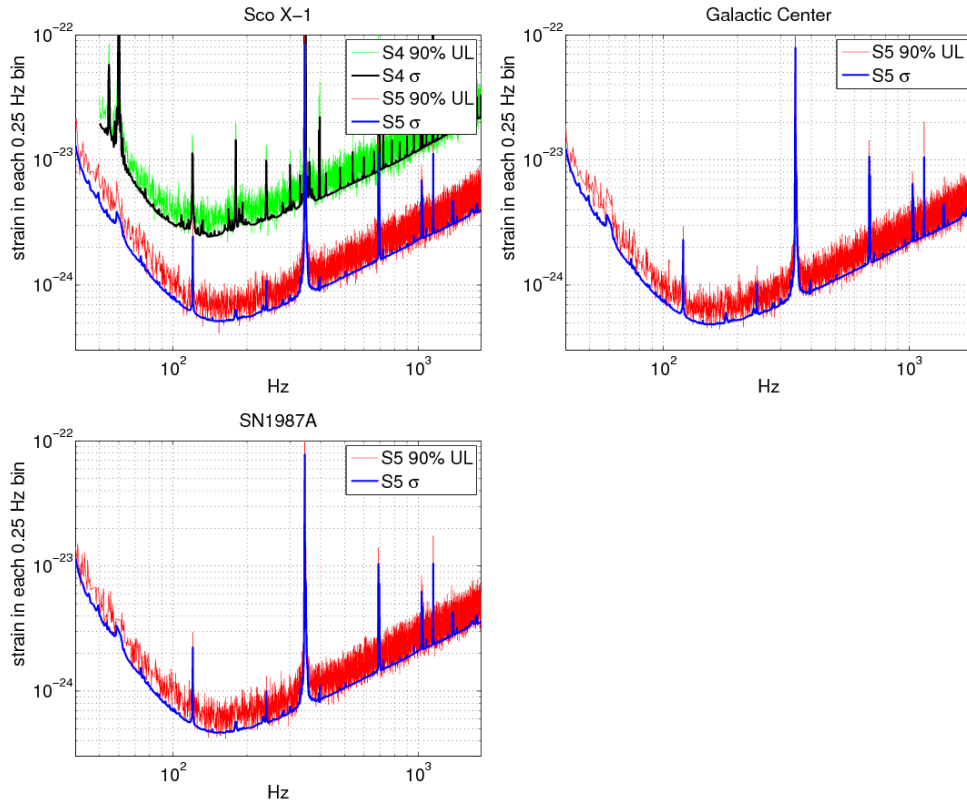


FIG. 4: Radiometer 90% upper limits on RMS strain in each 0.25 Hz wide bin as a function of frequency for Sco X-1 (top-left), the Galactic Center (top-right) and SN1987A (bottom). The large spikes correspond to harmonics of the 60 Hz power mains, calibration lines and suspension-wire resonances. The previous S4 upper limits for Sco X-1 [21] are also plotted in the top-left panel, illustrating the improvement in the upper limits obtained by using the LIGO S5 data. This is the first radiometer measurement of the Galactic Center and SN1987A.

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  - [37] The data were first processed with  $l_{\max} = 20$ ; the present method of choosing  $l_{\max}$  was then adopted a posteriori in order to more accurately model the angular resolution of the interferometer network.
  - [38] We follow the marginalization scheme used in [20], but note that this does not take into account covariance between baselines with a shared detector. Because the H2L1 baseline only contributes about 10% of the sensitivity, and the calibration uncertainty is on the order of 10% to start with, this effect is only on the order of 1%. Work is ongoing to take this effect into account, which we expect to be more important for baselines with comparable sensitivities.
  - [39] A prior constructed from [21] would be nearly flat anyway since the strain sensitivity has improved ten-fold since the S4 science run.